

Here are some BIC citations of interest:

Wasserman (2000) in J of Math Psych gives a formula (27) which implies that a BIC-related difference between two models is $\log B_{ij}$ where B is the Bayes factor for choosing between model i and j. Wasserman's (27) says that $\log B_{ij}$ is approximately what Mplus calls minus 1/2 BIC. This means that $2\log B_{ij}$ is in the Mplus BIC scale apart from the ignorable sign difference.

Kass and Raftery (1995) in J of the Am Stat Assoc gives rules of evidence on page 777 for $2\log_e B_{ij}$ which say that >10 is very strong evidence in favor of the model with largest value.

So, to conclude, this says that an Mplus BIC difference > 10 is strong evidence against the model with the highest Mplus BIC value (I hope I got that right).

Raftery has a Soc Meth chapter:

Raftery, A. E. (1995). Bayesian Model Selection in Social Research. Sociological Methodology, 25, 111-163.

that talks about B_{ij} from a SEM perspective.

There's also a good discussion about this here:

<http://www.statmodel.com/discussion/messages/23/2232.html?1209409498>

[Aaron M. Thompson](#) posted on Monday, August 30, 2010 - 6:14 pm
Dr. Muthen,

Thank you for the great resources. I hate to belabor this point, but I am a stickler for accuracy and I am an intervention researcher - not a mathematician. Last summer, I took an ICPSR course and learned about the Raftery citation for calculating a more interpretable BIC using the Mplus chi2 in the formula " $\chi^2 - df (\ln(N))$ ". This calculation produces a BIC that is comparable across nonnested models following the Raftery rule >10 .

However, as Mplus LTA output does not give a chi2, but only a LgLkd chi2, I am assuming that I can not use this statistic in this calculation, am I correct in my understanding?

Therefore, following your suggestions using the results from my models, $2\ln$ of the BIC (19355.681) for model $i = 19.741$, $2\ln$ of the BIC (18956.107) for model $j = 19.699$. The difference between B_{ij} is less than 10. Thus, according to your explanation, this is "strong" statistical evidence for retaining the more parsimonious model with the larger BIC (i.e. keep model i over model j). Is my interpretation of this accurate?

Thanks again for your time and consideration.

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Bengt O. Muthen posted on Tuesday, August 31, 2010 - 2:36 pm
Comparing models using the formula " χ^2 -df ($\ln(N)$)" is the same as using the Mplus
 $BIC = -2\log L + p \cdot \ln(N)$, where p is the number of parameters. Note that

$$\chi^2 = -2(\log L_a - \log L_b),$$

where a is a model nested within b . In the usual SEM case b is the totally unrestricted model called H1. Note also that

$$df = p_b - p_a,$$

where p is the number of parameters.

So when you look at the difference between the BIC of two models using the formula χ^2 -df ($\ln(N)$) there is a canceling out of the terms $-2\log L_b$ and of the terms $p_b \cdot \ln(N)$. This means that BIC differences are the same for both formulas. And this means that we should view a BIC difference > 10 as strong evidence that the model with lower BIC is better.