

Here are some BIC citations of interest:

Wasserman (2000) in J of Math Psych gives a formula (27) which implies that a BIC-related difference between two models is  $\log B_{ij}$  where B is the Bayes factor for choosing between model i and j. Wasserman's (27) says that  $\log B_{ij}$  is approximately what Mplus calls minus 1/2 BIC. This means that  $2\log B_{ij}$  is in the Mplus BIC scale apart from the ignorable sign difference.

Kass and Raftery (1995) in J of the Am Stat Assoc gives rules of evidence on page 777 for  $2\log_e B_{ij}$  which say that  $>10$  is very strong evidence in favor of the model with largest value.

So, to conclude, this says that an Mplus BIC difference  $> 10$  is strong evidence against the model with the highest Mplus BIC value (I hope I got that right).

Raftery has a Soc Meth chapter:

Raftery, A. E. (1995). Bayesian Model Selection in Social Research. Sociological Methodology, 25, 111-163.

that talks about  $B_{ij}$  from a SEM perspective.

There's also a good discussion about this here:

<http://www.statmodel.com/discussion/messages/23/2232.html?1209409498>

[Aaron M. Thompson](#) posted on Monday, August 30, 2010 - 6:14 pm  
Dr. Muthen,

Thank you for the great resources. I hate to belabor this point, but I am a stickler for accuracy and I am an intervention researcher - not a mathematician. Last summer, I took an ICPSR course and learned about the Raftery citation for calculating a more interpretable BIC using the Mplus chi2 in the formula " $\chi^2 - df (\ln(N))$ ". This calculation produces a BIC that is comparable across nonnested models following the Raftery rule  $>10$ .

However, as Mplus LTA output does not give a chi2, but only a LgLkd chi2, I am assuming that I can not use this statistic in this calculation, am I correct in my understanding?

Therefore, following your suggestions using the results from my models,  $2\ln$  of the BIC (19355.681) for model  $i = 19.741$ ,  $2\ln$  of the BIC (18956.107) for model  $j = 19.699$ . The difference between  $B_{ij}$  is less than 10. Thus, according to your explanation, this is "strong" statistical evidence for retaining the more parsimonious model with the larger BIC (i.e. keep model  $i$  over model  $j$ ). Is my interpretation of this accurate?

Thanks again for your time and consideration.

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Bengt O. Muthen posted on Tuesday, August 31, 2010 - 2:36 pm  
Comparing models using the formula " $\chi^2$ -df ( $\ln(N)$ )" is the same as using the Mplus BIC =  $-2\log L + p \cdot \ln(N)$ , where  $p$  is the number of parameters. Note that

$$\chi^2 = -2(\log L_a - \log L_b),$$

where  $a$  is a model nested within  $b$ . In the usual SEM case  $b$  is the totally unrestricted model called H1. Note also that

$$df = p_b - p_a,$$

where  $p$  is the number of parameters.

So when you look at the difference between the BIC of two models using the formula  $\chi^2$ -df ( $\ln(N)$ ) there is a canceling out of the terms  $-2\log L_b$  and of the terms  $p_b \cdot \ln(N)$ . This means that BIC differences are the same for both formulas. And this means that we should view a BIC difference  $> 10$  as strong evidence that the model with lower BIC is better.